

eISSN: 2581-9615 CODEN (USA): WJARAI Cross Ref DOI: 10.30574/wjarr Journal homepage: https://wjarr.com/

	WJARR W	USER 2564 4415 CODEN (1884) HUMAN
	World Journal of Advanced Research and Reviews	
		World Journal Series INDIA
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(REVIEW ARTICLE)

Transformative approaches and challenges in 21st century mathematics education: A comprehensive review

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World Journal of Advanced Research and Reviews, 2023, 20(03), 444-457

Publication history: Received on 29 October 2023; revised on 04 December 2023; accepted on 06 December 2023

Article DOI: https://doi.org/10.30574/wjarr.2023.20.3.2508

Abstract

This article examines the challenges and transformative approaches in 21st century mathematics education. The article examines the transition from conventional lecture-based teaching methods to more interactive, learner-focused strategies, with an emphasis on technology integration, mathematical literacy development, critical thinking, and tackling obstacles including math anxiety and gender inequalities. The article delves into innovative pedagogical strategies like flipped classrooms, gamification, and blended learning, highlighting their effectiveness in enhancing student engagement and understanding. It also underscores the importance of teacher training, parental involvement, and targeted interventions in creating an inclusive and empowering the mathematics classroom. The article concludes by emphasizing the need for educators to stay abreast of these promising and effective teaching strategies as education continues to evolve with technological advancements. The arguments put forth in this article are substantiated by recent research and advancements in the field of mathematics education.

Keywords: Mathematics Education in the 21st Century; Integration of Technology; Mathematical Literacy and Critical Thinking; Innovative Pedagogical Strategies; Overcoming Challenges in Mathematics Education

1. Introduction

The importance of transitioning from conventional lecture-based methods to more interactive, learner-focused strategies is becoming increasingly acknowledged within the field of mathematics education. This shift is necessitated by the evolving demands of the 21st-century workplace, which increasingly values creative problem-solving, adaptability, and technological proficiency. To meet these demands, mathematics education must evolve to offer students opportunities to engage in higher-order thinking, collaborative problem-solving, and the application of mathematical concepts in diverse contexts.

Innovation in mathematics education also necessitates the incorporation of technological advancements. Digital tools and resources have the potential to greatly augment the learning experience by offering visually stimulating and interactive materials that can assist in the clarification of intricate concepts. Technology also offers unique opportunities for differentiated instruction, facilitating self-paced learning and tailoring instructional approaches to accommodate individual learning styles. Furthermore, incorporating technology prepares students for a future where digital literacy is a fundamental skill.

In addition to these technological advancements, there is a growing emphasis on the importance of fostering a positive emotional and mental attitude towards mathematics. This includes promoting a growth mindset, where students are encouraged to view challenges as opportunities for learning and growth, rather than insurmountable obstacles. Developing a positive attitude towards mathematics is particularly crucial in early education, as it lays the foundation for future learning and interest in the subject.

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Another aspect of innovative mathematics education is the emphasis on real-world applications. By demonstrating how mathematical concepts are applied in various professional and everyday contexts, educators can make the subject more relatable and engaging. This approach not only enhances students' understanding and appreciation of mathematics, but also equips them with practical skills that they can apply in their future careers and daily lives.

In addition, collaborative learning is an integral component of cutting-edge mathematics education. Group activities and collaborative projects enable students to learn from one another, share different perspectives, and develop important social skills such as communication and teamwork. Students feel empowered to contribute and a more inclusive and supportive learning environment is fostered as a result of this method.

The challenges faced in mathematics education call for a comprehensive overhaul of traditional teaching methods. Innovative approaches should be holistic, encompassing not only the content and methods of instruction but also addressing the emotional, psychological, and practical aspects of learning mathematics. Educators can establish a more captivating, all-encompassing, and efficacious educational atmosphere that equips students for the intricacies of the contemporary era by implementing such extensive strategies.

2. Material and methods

This study employs a comprehensive literature review as both the material and methodology. The purpose of this approach is to synthesize and analyze the existing body of knowledge on transformative approaches and challenges in 21st-century mathematics education.

2.1. Materials

A diverse array of scholastic articles, research studies, and educational reports serve as the foundational sources for this investigation. These documents have been carefully selected to represent diverse perspectives and findings on the subject matter. The literature encompasses studies on traditional and innovative pedagogical strategies, the role of technology in education, mathematical literacy, critical thinking, and issues such as math anxiety and gender disparities in mathematics education.

2.2. Methodology

The methodology of this study involves several key steps:

- Identification of Sources: Relevant literature was identified through systematic searches of academic databases. The search strategy included a combination of keywords related to mathematics education, pedagogical strategies, technology integration, and related challenges.
- Selection and Evaluation: Each identified source was evaluated based on its relevance to the research topic, the credibility of the authors, and the quality of the research methods. Only the most reliable and pertinent sources were included in the review.
- Data Extraction: Key information was extracted from each source, including the research methods, findings, and conclusions. This data forms the basis for the analysis in this study.
- Analysis and Synthesis: The extracted data was analyzed to identify common themes, trends, and gaps in the existing research. This analysis was synthesized into a coherent narrative that presents an overview of the current state of knowledge on the topic.
- Interpretation: The final step involved interpreting the findings of the literature review in the context of the research objectives. This includes discussing the implications of the findings for educators, policy-makers, and future research.

This literature review methodology provides a robust framework for exploring and understanding the complex landscape of mathematics education in the 21st century. It allows for a thorough examination of the topic, ensuring that the insights and conclusions drawn are grounded in rigorous academic research.

3. Results

3.1. Mathematics Education Landscape from Past Studies

Recent studies and developments in mathematics education have brought about significant changes in how this subject is taught and learned. Several key factors have played a crucial role in shaping the landscape of mathematics education:

3.1.1. Impact of Technology

A study from the Universities of Surrey and Oxford, Loughborough University, and Radboud University in The Netherlands investigated the impact of neurostimulation on mathematical learning [1]. They found that electrical noise stimulation over the frontal part of the brain improved the mathematical ability of individuals with lower initial brain excitation. This suggests that neurostimulation could be a promising approach for enhancing mathematical learning in specific groups of learners.

The study you mentioned is indeed fascinating and sheds light on the potential of neurostimulation in enhancing mathematical learning. Neurostimulation, specifically electrical noise stimulation, involves applying small amounts of electrical current to specific areas of the brain. In this case, the stimulation was applied to the frontal part of the brain, an area associated with cognitive functions such as problem-solving, memory, and judgment.

The researchers found that this method improved the mathematical abilities of individuals who initially had lower brain excitation. This is a significant finding as it suggests that the brain's excitability level can influence learning outcomes. It also implies that neurostimulation could be tailored to individual needs, potentially helping those who struggle with mathematical learning.

Moreover, this study opens up new avenues for research in the field of education and cognitive neuroscience. If neurostimulation can enhance mathematical learning, it might also be beneficial for other areas of learning. For instance, it could potentially improve language acquisition, memory retention, or even artistic abilities. However, more research is needed to explore these possibilities and to understand the long-term effects and ethical implications of neurostimulation.

the study presents a promising approach to enhancing mathematical learning in specific groups of learners. It highlights the potential of neurostimulation as a tool for personalized education, paving the way for more inclusive and effective learning strategies. However, as with any new technology, it's important to proceed with caution and conduct further research to ensure its safe and ethical use.

3.1.2. Inquiry-Based Learning (IBL)

IBL is a learner-centered approach that starts with an essential question and involves learners actively in both the learning and decision-making processes [2]. It is a learner-centered approach that starts with an essential question and involves learners actively in both the learning and decision-making processes [3]. It's particularly effective for younger learners due to its appeal to their inquisitive nature [4,5]. IBL is flexible, allowing students to explore topics in various ways and through different media, including video, audio, and texts [6,7].

IBL is flexible, allowing students to explore topics in various ways and through different media, including video, audio, and texts [8,9]. It usually follows a cycle of Question & Plan, Research & Discover, Organise & Present, and Reflect [4, 5,10]. A study published in the Universal Journal of Educational Research found that students who were instructed through the inquiry-based learning method achieved higher scores than those instructed through the traditional method [3]. This suggests that IBL not only engages students but also enhances their academic performance.

Moreover, large-scale implementations of effective inquiry-based learning are rare. However, a European-wide initiative gave teachers access to innovative e-learning tools for lesson planning and classroom implementation [11]. These tools ranged from virtual labs, virtual games, and simulations to augmented reality applications. Teachers were encouraged to adopt five different phases of inquiry-based learning: orientation, hypothesizing, planning, analysis, and conclusion [11]. This initiative resulted in significant learning outcomes for participating students [11]. In the future, the basic infrastructure of schools may include resource centers operating under a superordinate management structure to encourage structured and open learning activities6. This would further enhance the implementation of IBL in classrooms, providing students with a more engaging and effective learning experience [11].

IBL with its focus on student engagement and active learning, is a powerful educational approach. It not only caters to the inquisitive nature of younger learners but also prepares them for the demands of the 21st-century world by fostering critical thinking and problem-solving skills. The integration of technology in this approach further enhances its effectiveness, making learning a more interactive and enriching experience for students.

3.1.3. Collaborative Approaches

Collaborative learning indeed plays a crucial role in modern educational strategies. It involves group activities and projects, allowing students to learn from each other, share perspectives, and develop social skills like communication and teamwork.

In 2023, a study titled "Collaboration between Mathematicians and Mathematics Educators: dialogical inquiry as a methodological tool in Mathematics Education research" was published in the Educational Studies in Mathematics journal [12]. The study emphasized the importance of collaboration between mathematicians and mathematics educators in advancing knowledge on the teaching and learning of Mathematics, particularly in advanced Mathematics pedagogy [12]. The researchers presented a novel methodology for collaborative inquiry and qualitative data analysis— dialogical inquiry —based on Mikhail Bakhtin's theory of dialogism [12]. This methodology opened a "dialogical space" where ideas could be discussed, voices were heard equally, and as a result, shared meanings emerged [12].

Another study titled "Future themes of mathematics education research: an international survey before and during the pandemic" was also published in the Educational Studies in Mathematics journal [13]. Although this study was not specifically focused on collaborative learning, it did highlight the importance of various themes in mathematics education research, including teaching approaches, goals, relations to practices outside mathematics education, teacher professional development, technology, affect, equity, and assessment [13].

3.1.4. Real-World Applications

Integrating real-world applications in mathematics education is indeed increasingly emphasized to make the subject more relatable and engaging for students. This approach not only enhances understanding and appreciation of mathematics but also equips students with practical skills they can apply in their future careers and daily lives.

A study titled "Connecting Mathematics To Real Life Problems: A Teaching Quality That Improves Students' Mathematics Interest" published in the IOSR Journal of Research & Method in Education emphasizes the importance of connecting mathematical concepts to real-life problems [14]. The study found that students' interest in Mathematics increases when teachers dedicate quality time for practicing class exercises and are able to link Mathematics to other subject areas [14].

The findings suggest that when mathematical concepts are connected to real-life problems, students' interest in the subject increases. This is likely because students can see the practical relevance of what they are learning, which makes the learning experience more engaging and meaningful.

Moreover, the study highlights the importance of quality time dedicated to practicing class exercises and linking Mathematics to other subject areas. This interdisciplinary approach not only deepens students' understanding of mathematical concepts but also allows them to see the interconnectedness of different fields of knowledge.

However, it's important to note that the successful implementation of this approach requires careful planning and execution. Teachers need to select real-world problems that are appropriate for their students' level of understanding and are aligned with the learning objectives of the course. They also need to provide adequate support and guidance to help students make connections between the mathematical concepts and the real-world problems.

Another study titled "Bringing Math to Life: Provide Students Opportunities to Connect their Lives to Math" published in Networks: An Online Journal for Teacher Research examined the use of math journals by fourth-grade students as a conduit for critical thinking, reflection, and real-world math application [15]. The study found that students made a deeper connection to math's many real-life applications in their own lives [15].

The use of math journals in this study allowed fourth-grade students to engage in critical thinking and reflection, which are key components of deep learning. By writing about their mathematical thoughts and experiences, students were able to make connections between the mathematical concepts they were learning in school and their everyday lives.

This finding underscores the importance of making mathematics relevant to students' lives. When students see how mathematical concepts apply to real-world situations, they are more likely to find the subject interesting and meaningful. This, in turn, can lead to improved engagement and achievement in mathematics.

Moreover, the use of math journals can also help teachers gain insights into their students' thinking processes, which can inform their teaching strategies and help them provide more targeted support to their students.

These studies underscore the significance of integrating real-world applications in mathematics education and provide valuable insights into how this approach can be effectively implemented to enhance student learning outcomes. By making mathematics more relatable and engaging, we can foster a deeper understanding and appreciation of the subject, equipping students with practical skills they can apply in their future careers and daily lives.

3.1.5. Socio-Cultural Factors

The socio-cultural environment in which students learn mathematics significantly influences their learning experience. This is because learning is not an isolated process; it is deeply intertwined with the social and cultural contexts in which it occurs [16]. Understanding these factors is vital for developing teaching strategies that are culturally responsive and inclusive.

For instance, Vygotsky's Sociocultural Theory emphasizes that the development of a child's higher mental processes depends on the presence of mediating agents in the child's interaction with the environment [17]. This theory underscores the importance of the socio-cultural context in shaping the learning experience.

Moreover, research has shown that more than individual aspirations or learning abilities, contextual factors such as social environment, caste or community background, habitation, workplaces, neighborhood with its socio-cultural features, and the type of school where children study are likely to determine the trajectory of learning in general and mathematics learning in particular [16].

In light of these insights, it becomes crucial to develop teaching strategies that are culturally responsive and inclusive. Culturally Responsive Teaching (CRT) in mathematics involves working with learners' parents and families for mathematizing contexts, creating and adapting mathematical problems, utilizing questioning strategies to elicit learners' local knowledge, requiring explanation and justification as it relates to context knowledge, and creating project-based opportunities incorporating funds of knowledge.

Furthermore, it is important to recognize and incorporate diverse ways of doing math, showing diverse people doing math, and contextualizing math within relevant societal issues that students can connect to their own lives. This approach not only makes learning more engaging for students but also helps in building a more inclusive and equitable learning environment.

3.1.6. Innovative Pedagogical Approaches

In recent years, the educational landscape has seen a surge in innovative pedagogical approaches, particularly within mathematics education. One such approach is the flipped classroom, which reverses the traditional teaching method. Instead of delivering lectures in class and assigning homework to be done outside, students watch lectures or read materials at home and engage in interactive activities during class. This reversal has proven to enhance individualized instruction, as teachers can spend class time addressing specific challenges. Research supports that students in flipped classrooms often display improved academic performance and higher engagement.

The flipped classroom is an innovative pedagogical approach that has been gaining popularity, especially in mathematics education. This method reverses the traditional teaching model. Instead of delivering lectures in class and assigning homework to be done outside, students watch lectures or read materials at home and engage in interactive activities during class.

This approach has several benefits:

- Personalized and self-paced learning: Students can learn at their own pace, reviewing any part of a recorded lecture or taking breaks as needed.
- More time for interactive learning situations: Class time is used for interactive activities, allowing for more hands-on learning.
- Responsibility for learning: Students take control of their own learning, which can be empowering.
- Critical thinking and collaboration: The interactive nature of the classroom activities often requires students to engage in critical thinking and work together.
- Improved student engagement: The flipped classroom model has been found to increase student engagement.
- Improved student understanding: With the ability to review lectures at their own pace, students may have a better understanding of the material.

Research supports that students in flipped classrooms often display improved academic performance and higher engagement. However, it's important to note that the success of a flipped classroom can depend on various factors, such as the quality of the lectures and the level of student preparation. It's not a silver bullet for instantly boosting course evaluations, but it does offer a new approach to teaching and learning that can be highly beneficial in the right circumstances.

Some key points about the flipped classroom approach:

- The flipped classroom model allows students to learn at their own pace, encourages students to actively engage with lecture material, frees up actual class time for more effective, creative and active learning activities [18].
- The most frequently reported advantage of the flipped classroom is the improvement of student learning performance [19].
- The flipped classroom teaching model can enhance students' self-reliant and active learning, increase collaboration, and improve learning outcomes [20].
- The flipped classroom approach has a positive effect on learning, reducing cognitive load, involvement, accuracy, motivation, attitude, and satisfaction with the course and self-efficacy in higher education [21].

However, it's important to note that the success of a flipped classroom can depend on various factors, such as the quality of the lectures and the level of student preparation [19]. It's not a silver bullet for instantly boosting course evaluations, but it does offer a new approach to teaching and learning that can be highly beneficial in the right circumstances [19].

Another transformative approach is gamification, gamification in education is a transformative approach that incorporates game-like elements such as points, badges, and leaderboards into non-game contexts, like math lessons [22,23]. This method has turned learning into a more engaging activity, especially for students who find traditional methods monotonous [22,23,24,25]. The 'game' aspect motivates participation and achievement [22,23,24].

Here are some key points about gamification in education:

- Gamification research in educational settings has produced mixed results on student learning outcomes [26]. Educational researchers and practitioners both struggle with identifying when, where, and how to use gamification design concepts [26,27].
- The systematic review demonstrates that the application of gamification in learning has a favorable effect on the improvement of motivation scores and their engagement during the teaching and learning process [22,28]. Gamification in education is especially promising due to its ability to influence students' behavior in a favorable manner.
- The impact of gamification on students' learning, engagement, and behavior based on their personality traits [29]. The gamification of education can enhance levels of students' engagement similar to what games can do, to improve their particular skills and optimize their learning [29].

Studies have highlighted increased motivation, engagement, and retention in gamified learning environments [18,19,20]. However, it's important to note that the success of gamification can depend on various factors, such as the quality of the game elements and the level of student preparation [20]. It's not a silver bullet for instantly boosting course evaluations, but it does offer a new approach to teaching and learning that can be highly beneficial in the right circumstances [20].

Lastly, blended learning, which seamlessly integrates traditional face-to-face instruction with online learning, offers a flexible and adaptive model. Students might attend some sessions in person while completing online modules at other times, catering to different learning styles and paces. The ability to revisit online materials ensures students thoroughly understand concepts. Multiple studies have found blended learning to be exceptionally effective, with students demonstrating a deeper grasp of mathematical concepts compared to exclusively traditional or online methods. In essence, as education continues to evolve, it's imperative for educators to stay abreast of these promising and effective teaching strategies.

Here are some key points about blended learning:

• Blended learning (BL) has increasingly been utilized in higher education as it has the advantages of both traditional and online teaching approaches [30,31]. It enhances students' learning engagement and experience

as it creates a significant influence on students' awareness of the teaching mode and learning background [31,32].

- Blended learning moves the emphasis from teaching to learning, thus enabling students to become more involved in the learning process and more enthused and, consequently, improves their perseverance and commitment [31].
- There has been rapid development in BL adoption focused on improving teaching and learning outcome. Prior studies assessed the effectiveness of BL by comparing the traditional teaching and online teaching [33,34,35].

4. Blended learning (BL), or the integration of face-to-face and online instruction, is widely adopted across higher education with some scholars referring to it as the "new traditional model" or the "new normal" in course delivery [36]. In considering effectiveness, the authors contend that BL coalesces around access, success, and students' perception of their learning environments [36].

Multiple studies have found blended learning to be exceptionally effective, with students demonstrating a deeper grasp of mathematical concepts compared to exclusively traditional or online methods. As education continues to evolve, it's imperative for educators to stay abreast of these promising and effective teaching strategies.

3.1.7. Technology Integration in Mathematics Education

Advancements in technology have transformed the learning landscape. This section discusses the role of digital tools, simulations, and online platforms in mathematics education. It explores how adaptive learning technologies and artificial intelligence can personalize learning experiences, catering to individual student needs and promoting mastery of mathematical skills.

The rapid pace of technological advancements has ushered in a new era for education, particularly in the realm of mathematics. Digital tools, once considered supplementary, are now at the forefront of pedagogical strategies, offering a plethora of opportunities for interactive and dynamic learning [37,38,39].

Simulations, for instance, allow students to visualize and experiment with mathematical concepts in real-time, providing a tangible understanding that traditional methods might not afford [37,38,39]. These virtual environments enable learners to witness the practical applications of abstract theories, bridging the gap between knowledge and its real-world relevance[37,38,39]. According to a study, simulations serve as approximations of practice that provide opportunities for learners to try out new learning practices in a safe space[37]. Another study found that simulation-based materials not only improved students' problem-solving skills and scores but also resulted in students' development of favorable attitudes towards the instructional approach[39].

Online platforms, on the other hand, have democratized access to high-quality resources and expertise [40,41,42,43]. With platforms ranging from video lectures and tutorials to comprehensive courses, students from all over the world can now engage with content from renowned educators and institutions [40,41,42]. This global access ensures that geography is no longer a barrier to top-tier mathematical education [41,42,43]. A study found that online learning helps ensure that e-learning can be easily managed, and the learner can easily access the teachers and teaching materials [44]. It also helped reduce the effort and travel expenses and other expenses that accompany traditional learning [44].

However, one of the most groundbreaking integrations into the educational sphere has been adaptive learning technologies powered by artificial intelligence [45,46,47,48,49]. Unlike one-size-fits-all curriculums, adaptive learning systems are designed to adjust the content, resources, and exercises in real-time based on individual student performance and needs [45,46,47,48,49]. This means that each student's learning path can be uniquely tailored, addressing their specific strengths and weaknesses [45,46,47,48,49]. For instance, if a student struggles with algebraic equations, the system might provide additional resources or exercises in that particular area until the student demonstrates proficiency [45,46,47,48,49].

Furthermore, AI-driven platforms can also offer immediate feedback, allowing students to identify and rectify mistakes promptly [50,51,52,53]. This immediate feedback loop not only enhances understanding but also boosts confidence, as students can see their progression and mastery over time [50,51,52,53]. A study found that AI systems could be supportive of student engagement because the students are getting real-time answers [51]. Another study found that AI-powered tools make learning accessible for all students, anytime and anywhere [52].

The integration of digital tools, online platforms, and AI-driven adaptive learning technologies into the educational sphere has revolutionized the way students learn, especially in the field of mathematics. These advancements have made learning more interactive, dynamic, and personalized, thereby enhancing students' understanding and mastery of mathematical concepts. As education continues to evolve with technological advancements, it's imperative for educators to stay abreast of these promising and effective teaching strategies [37,38,39,46,47,50,51,52,53].

3.1.8. Fostering Mathematical Literacy and Critical Thinking

Developing mathematical literacy and critical thinking skills is essential for students to succeed in the 21st century [54,55,56]. This section discusses strategies to foster these skills, including problem-based learning, mathematical modeling, and collaborative problem-solving activities. It also explores the role of assessments in promoting higher-order thinking skills among students [57,58,59].

In our modern, rapidly evolving world, it's crucial for students to possess strong mathematical literacy and critical thinking skills to navigate the complexities of the 21st century [54,55,56]. Mathematical literacy extends beyond basic arithmetic; it embodies the ability to apply mathematical concepts to real-world scenarios, reason effectively, and communicate solutions [54,55,56].

One transformative approach to cultivating this skill is through Problem-Based Learning (PBL). Unlike traditional methods, PBL immerses students in real-world challenges, demanding active engagement and application of mathematical principles [54,55,56]. A study found that students' attitudes and achievements improved through problem-based learning in mathematics [54]. Another study found that problem-solving instruction creates opportunities for students to apply their knowledge of mathematical concepts, integrate and connect isolated pieces of mathematical knowledge, and attain a deeper conceptual understanding of mathematics as a subject [56]. Alongside mathematical literacy, fostering critical thinking in students is paramount. This extends beyond simple calculations, urging students to question assumptions, evaluate diverse solutions, and form reasoned conclusions [54,55,56].

A potent tool in this endeavor is mathematical modeling. This acts as a conduit between theoretical math and tangible, real-world applications [60,61,62]. Through modeling, students can encapsulate complex problems in mathematical terms, offering a systematic approach to challenges [60,61,62]. A study found that through mathematical modeling, students can generate mathematical ideas, explore mathematical theorems independently, develop critical thinking, and improve their metacognitive and communicative skills [60].

Additionally, the realm of mathematics, often perceived as a solitary pursuit, gains immense value through collaborative problem-solving [63,64,65]. As students collaborate, they pool diverse perspectives, challenge each other's logic, and converge on holistic solutions, enriching their understanding and honing interpersonal skills [63,64,65]. A study found that collaboration for problem-solving provides some benefits, such as a more effective division of labor and the incorporation of differing perspectives, knowledge, and experiences [63]. Another study found that the activities improved students' problem-solving skills and productivity and encouraged them to work collaboratively [65].

Lastly, the role of assessments in this learning journey is pivotal. Modern assessments have evolved from mere retention tests to tools that emphasize critical analysis and problem-solving [57,58,59]. Crafted thoughtfully, they can push students towards deeper cognitive engagement, ensuring not just rote learning but genuine comprehension [57,58,59]. A study found that the integration of higher-order thinking skills (HOTS) in language learning assessments has become a crucial issue in 21st-century learning4. Another study found that the assessments improved students' problem-solving skills and productivity and encouraged them to work collaboratively [57,58].

3.1.9. Overcoming Challenges in Mathematics Education

Addressing challenges in mathematics education, such as math anxiety and gender disparities, is crucial for creating an inclusive learning environment. This section discusses strategies to overcome these challenges, emphasizing the importance of teacher training, parental involvement, and targeted interventions [66,67,68,69,70].

Mathematics, often perceived as a purely logical discipline, is intertwined with social and emotional aspects of learning. Issues like math anxiety, a persistent fear or apprehension towards the subject, can hinder a student's performance, confidence, and overall interest in mathematics [69,70]. Similarly, gender disparities, a longstanding issue in STEM (Science, Technology, Engineering, and Mathematics) fields, can deter certain demographics from pursuing advanced mathematical studies and careers [71,72,73,74]. Creating an inclusive mathematics learning environment is paramount to tackling these challenges. An environment where every student, regardless of their background or personal struggles, feels valued, understood, and capable of success.

One of the foundational pillars in overcoming these challenges is teacher training [75,76]. Educators equipped with the right tools, strategies, and understanding can identify signs of math anxiety early and deploy effective pedagogical methods to mitigate it [69,70]. For instance, integrating more collaborative and hands-on problem-solving sessions can make math more approachable and less intimidating [77]. Moreover, trained educators can actively challenge and dismantle gender biases, creating classrooms that celebrate diversity and promote equal opportunities for all students [71,72,73,74].

Parental involvement plays a pivotal role as well [66,67,68]. Parents and guardians, as primary influencers in a child's life, can reinforce positive attitudes towards mathematics. By engaging in math-related activities at home, showing enthusiasm about the subject, and providing necessary support, parents can counteract negative stereotypes and anxieties related to math [66,67,68].

Targeted interventions, such as one-on-one tutoring or counseling, can offer tailored solutions to students grappling with specific issues [69,70]. For those with severe math anxiety, cognitive-behavioral therapies and resilience-building exercises might be beneficial [69,70]. Meanwhile, initiatives like mentorship programs or all-girls math clubs can provide a supportive community for those affected by gender disparities, allowing them to thrive in an environment that recognizes and celebrates their potential [71,72,73,74].

4. Discussion

The discussion on the transformative approaches and challenges in mathematics education in the 21st century, as presented in this paper, brings to light several key aspects of modern educational practices.

Firstly, the shift from traditional, lecture-based instruction to more dynamic, student-centered approaches is a significant change in the pedagogical landscape. This shift is characterized by the integration of innovative strategies like flipped classrooms, gamification, and blended learning, which leverage technology to enhance student engagement and deepen their understanding of mathematical concepts.

Secondly, there is a growing emphasis on fostering mathematical literacy and critical thinking skills. These skills are essential for students to navigate the complexities of the modern world. Addressing challenges such as math anxiety and gender disparities is crucial for creating an inclusive learning environment. Strategies to overcome these challenges include teacher training, parental involvement, and targeted interventions.

Thirdly, the role of technology in mathematics education is becoming increasingly important. Digital tools, online platforms, and AI-driven adaptive learning technologies are revolutionizing the way students learn. These advancements have made learning more interactive, dynamic, and personalized, thereby enhancing students' understanding and mastery of mathematical concepts.

However, the integration of these transformative approaches and technologies also presents several challenges. For instance, teachers need to be adequately trained to use these tools effectively. Additionally, there is a need for ongoing research to evaluate the effectiveness of these approaches and to identify areas for improvement.

This paper highlights the need for a multifaceted approach to mathematics education in the 21st century. This approach should integrate innovative pedagogical strategies, foster mathematical literacy and critical thinking, address educational challenges, and leverage technology to enhance learning outcomes. As education continues to evolve with technological advancements, it's imperative for educators to stay abreast of these promising and effective teaching strategies.

5. Conclusion

In conclusion, the landscape of mathematics education in the 21st century is undergoing a significant transformation. The shift from traditional, lecture-based instruction to more dynamic, student-centered approaches is becoming increasingly prevalent. These approaches, including flipped classrooms, gamification, and blended learning, leverage technology to enhance student engagement and deepen their understanding of mathematical concepts.

Moreover, there is a growing emphasis on fostering mathematical literacy and critical thinking skills, which are essential for students to navigate the complexities of the modern world. Addressing challenges such as math anxiety and gender disparities is also crucial for creating an inclusive learning environment. Strategies to overcome these challenges include teacher training, parental involvement, and targeted interventions.

The integration of digital tools, online platforms, and AI-driven adaptive learning technologies into the educational sphere has revolutionized the way students learn, especially in the field of mathematics. These advancements have made learning more interactive, dynamic, and personalized, thereby enhancing students' understanding and mastery of mathematical concepts.

As education continues to evolve with technological advancements, it's imperative for educators to stay abreast of these promising and effective teaching strategies. The insights presented in this article, supported by recent studies and developments in mathematics education, highlight the importance of adopting such multifaceted approaches to create a more engaging, inclusive, and effective learning environment that prepares students for the complexities of the modern world.

References

- [1] N. E. R. van Bueren, S. H. G. van der Ven, S. Hochman, F. Sella, and R. Cohen Kadosh, "Human neuronal excitation/inhibition balance explains and predicts neurostimulation induced learning benefits," *PLOS Biol.*, vol. 21, no. 8, p. e3002193, Aug. 2023, doi: 10.1371/journal.pbio.3002193.
- [2] A. Gholam, "Inquiry-Based Learning: Student Teachers' Challenges and Perceptions," *J. Inq. Action Educ.*, vol. 10, no. 2, p. 2019.
- [3] A. Abdi, "The Effect of Inquiry-based Learning Method on Students' Academic Achievement in Science Course," *Univers. J. Educ. Res.*, vol. 2, no. 1, pp. 37–41, Jan. 2014, doi: 10.13189/ujer.2014.020104.
- [4] M. Worgan, "Inquiry-based learning: make your classroom more inclusive," 2023. https://www.cambridge.org/elt/blog/2023/01/08/inquiry-based-learning-make-your-classroom-moreinclusive/ (accessed Dec. 01, 2023).
- [5] D. A. Urdanivia Alarcon, F. Talavera-Mendoza, F. H. Rucano Paucar, K. S. Cayani Caceres, and R. Machaca Viza, "Science and inquiry-based teaching and learning: a systematic review," *Front. Educ.*, vol. 8, May 2023, doi: 10.3389/feduc.2023.1170487.
- [6] M. A. Al Mamun and G. Lawrie, "Student-content interactions: Exploring behavioural engagement with self-regulated inquiry-based online learning modules," *Smart Learn. Environ.*, vol. 10, no. 1, p. 1, Jan. 2023, doi: 10.1186/s40561-022-00221-x.
- [7] P. Levy, S. Little, and P. McKinney, *The Sheffield Companion to Inquiry-Based Learning*. CILASS: The Centre for Inquirybased Learning in the Arts and Social Sciences, Sheffield, 2010. [Online]. Available: https://eprints.whiterose.ac.uk/192004/1/Sheffield_IBL_Companion.pdf
- [8] C. Attard, N. Berger, and E. Mackenzie, "The Positive Influence of Inquiry-Based Learning Teacher Professional Learning and Industry Partnerships on Student Engagement With STEM," *Front. Educ.*, vol. 6, Aug. 2021, doi: 10.3389/feduc.2021.693221.
- [9] N. Ismail, S. Alias, and I. mohd ariff albakri, "Inquiry-Based Learning: A New Approach to Classroom Learning," *English Lang. J.*, vol. 2, p. 2006, Jan. 2006.
- [10] M. Pedaste *et al.*, "Phases of inquiry-based learning: Definitions and the inquiry cycle," *Educ. Res. Rev.*, vol. 14, pp. 47–61, Feb. 2015, doi: 10.1016/j.edurev.2015.02.003.
- [11] S. A. Sotiriou, A. Lazoudis, and F. X. Bogner, "Inquiry-based learning and E-learning: how to serve high and low achievers," *Smart Learn. Environ.*, vol. 7, no. 1, p. 29, Dec. 2020, doi: 10.1186/s40561-020-00130-x.
- [12] P. Hernandez-Martinez, S. Rogovchenko, Y. Rogovchenko, and S. Treffert-Thomas, "Collaboration between Mathematicians and Mathematics Educators: dialogical inquiry as a methodological tool in Mathematics Education research," *Educ. Stud. Math.*, vol. 114, no. 1, pp. 129–148, Sep. 2023, doi: 10.1007/s10649-023-10245w.
- [13] A. Bakker, J. Cai, and L. Zenger, "Future themes of mathematics education research: an international survey before and during the pandemic," *Educ. Stud. Math.*, vol. 107, no. 1, pp. 1–24, May 2021, doi: 10.1007/s10649-021-10049-w.
- [14] Y. D. Arthur, E. K. Owusu, S. K. Asiedu-Addo, and A. K. Arhin, "Connecting Mathematics To Real Life Problems : A Teaching Quality That Improves Students ' Mathematics Interest," 2018. [Online]. Available: https://api.semanticscholar.org/CorpusID:201639252
- [15] C. D. Benson-O'Connor, C. McDaniel, and J. Carr, "Bringing Math to Life: Provide Students Opportunities to

Connect their Lives to Math," Networks An Online J. Teach. Res., vol. 21, no. 2, Jan. 2019, doi: 10.4148/2470-6353.1299.

- [16] A. Bose and V. K. Kantha, "Influence of socio-economic background and cultural practices on mathematics education in India: a contemporary overview in historical perspective," *ZDM*, vol. 46, no. 7, pp. 1073–1084, Dec. 2014, doi: 10.1007/s11858-014-0607-x.
- [17] J. T. Kinard and A. Kozulin, "Vygotsky's Sociocultural Theory and Mathematics Learning," in *Rigorous Mathematical Thinking*, Cambridge University Press, 2008, pp. 50–72. doi: 10.1017/CB09780511814655.004.
- [18] J. Nouri, "The flipped classroom: for active, effective and increased learning especially for low achievers," *Int. J. Educ. Technol. High. Educ.*, vol. 13, no. 1, p. 33, Dec. 2016, doi: 10.1186/s41239-016-0032-z.
- [19] G. Akçayır and M. Akçayır, "The flipped classroom: A review of its advantages and challenges," *Comput. Educ.*, vol. 126, pp. 334–345, Nov. 2018, doi: 10.1016/j.compedu.2018.07.021.
- [20] S. E. E. Purba, K. Kristiani, K. B. Sangka, and O. K. Hussain, "The Flipped Classroom: An Overview of its Impact on Economics Learning," *Int. J. Pedagog. Teach. Educ.*, vol. 5, no. 1, p. 26, May 2021, doi: 10.20961/ijpte.v5i1.49750.
- [21] S. Han, "Flipped classroom: Challenges and benefits of using social media in English language teaching and learning," *Front. Psychol.*, vol. 13, Sep. 2022, doi: 10.3389/fpsyg.2022.996294.
- [22] C. Dichev and D. Dicheva, "Gamifying education: what is known, what is believed and what remains uncertain: a critical review," *Int. J. Educ. Technol. High. Educ.*, vol. 14, no. 1, p. 9, Dec. 2017, doi: 10.1186/s41239-017-0042-5.
- [23] L. F. Rodrigues, A. Oliveira, and H. Rodrigues, "Main gamification concepts: A systematic mapping study," *Heliyon*, vol. 5, no. 7, p. e01993, Jul. 2019, doi: 10.1016/j.heliyon.2019.e01993.
- [24] A. Christopoulos and S. Mystakidis, "Gamification in Education," *Encyclopedia*, vol. 3, no. 4, pp. 1223–1243, Oct. 2023, doi: 10.3390/encyclopedia3040089.
- [25] I. Aldalur and A. Perez, "Gamification and discovery learning: Motivating and involving students in the learning process," *Heliyon*, vol. 9, no. 1, p. e13135, Jan. 2023, doi: 10.1016/j.heliyon.2023.e13135.
- [26] R. Huang *et al.*, "The impact of gamification in educational settings on student learning outcomes: a metaanalysis," *Educ. Technol. Res. Dev.*, vol. 68, Jul. 2020, doi: 10.1007/s11423-020-09807-z.
- [27] N. Zeybek and E. Saygı, "Gamification in Education: Why, Where, When, and How?—A Systematic Review," *Games Cult.*, p. 155541202311586, Mar. 2023, doi: 10.1177/15554120231158625.
- [28] M. L. Hasan, M. E. Mohyaldinn, N. A. Hja Aziz, and M. A. Mohamed, "Improving Students' Motivation to Learn through Gamification," in 2017 7th World Engineering Education Forum (WEEF), Nov. 2017, pp. 642–647. doi: 10.1109/WEEF.2017.8467059.
- [29] R. Smiderle, S. J. Rigo, L. B. Marques, J. A. Peçanha de Miranda Coelho, and P. A. Jaques, "The impact of gamification on students' learning, engagement and behavior based on their personality traits," *Smart Learn. Environ.*, vol. 7, no. 1, p. 3, Dec. 2020, doi: 10.1186/s40561-019-0098-x.
- [30] J. Website, I. Ridayanti, A. Halim, and F. H. Amin, "International Journal of Business, English, and Communication THE IMPLEMENTATION OF BLENDED LEARNING IN THE EFL CLASSROOM AT SMA NEGERI 4 SELAYAR," *Int. J. Business, English, Commun.*, vol. 1, no. 2, pp. 68–76, 2023.
- [31] B. Anthony *et al.*, "Blended Learning Adoption and Implementation in Higher Education: A Theoretical and Systematic Review," *Technol. Knowl. Learn.*, vol. 27, no. 2, pp. 531–578, Jun. 2022, doi: 10.1007/s10758-020-09477-z.
- [32] H. Shenkut, M. Atnafu, and M. Woldemichael, "The Effect of Blended Learning Approach on Students' Engagement in Learning Algebra," vol. 25, pp. 193–198, Nov. 2023.
- [33] S. Suwannaphisit, C. Anusitviwat, P. Tuntarattanapong, and C. Chuaychoosakoon, *Comparing The Effectiveness of Blended Learning and Traditional Learning in An Orthopedics Course.* 2021. doi: 10.21203/rs.3.rs-852260/v1.
- [34] K. K. Trivedi, "Blended Learning: A Combination of Traditional and Online Teaching Learning," *Int. J. Adv. Res. Sci. Commun. Technol.*, pp. 222–225, Apr. 2021, doi: 10.48175/IJARSCT-1015.
- [35] E. Bergmans, A. Billington, and K.-C. Thies, "From tradition to innovation: a comparison of the traditional 4-step approach versus a blended learning modification for technical skills teaching," *Scand. J. Trauma. Resusc. Emerg. Med.*, vol. 31, no. 1, p. 80, Nov. 2023, doi: 10.1186/s13049-023-01127-4.

- [36] D. Prasetyo, B. Wibawa, and A. O. Dima, "Blended Learning implementation in introduction to artificial intelligence courses using the System Development Life Cycle method," *IOP Conf. Ser. Mater. Sci. Eng.*, vol. 1098, no. 4, p. 042001, Mar. 2021, doi: 10.1088/1757-899X/1098/4/042001.
- [37] J. N. Mikeska, H. Howell, L. Dieker, and M. Hynes, "Understanding the role of simulations in k-12 mathematics and science teacher education: Outcomes from a teacher education simulation conference," *Contemp. Issues Technol. Teach. Educ.*, vol. 21, no. 3, 2021.
- [38] O. Chernikova, N. Heitzmann, M. Stadler, D. Holzberger, T. Seidel, and F. Fischer, "Simulation-Based Learning in Higher Education: A Meta-Analysis," *Rev. Educ. Res.*, vol. 90, no. 4, pp. 499–541, Aug. 2020, doi: 10.3102/0034654320933544.
- [39] R. Taibu, L. Mataka, and V. Shekoyan, "Using PhET simulations to improve scientific skills and attitudes of community college students," *Int. J. Educ. Math. Sci. Technol.*, vol. 9, no. 3, pp. 353–370, 2021, doi: 10.46328/IJEMST.1214.
- [40] Z. Almahasees, K. Mohsen, and M. O. Amin, "Faculty's and Students' Perceptions of Online Learning During COVID-19," *Front. Educ.*, vol. 6, May 2021, doi: 10.3389/feduc.2021.638470.
- [41] M. Alzahrani, "Traditional Learning Compared to Online Learning During the COVID-19 Pandemic: Lessons Learned From Faculty's Perspectives," SAGE Open, vol. 12, no. 2, p. 215824402210917, Apr. 2022, doi: 10.1177/21582440221091720.
- [42] T. Hongsuchon, I. M. M. El Emary, T. Hariguna, and E. M. A. Qhal, "Assessing the Impact of Online-Learning Effectiveness and Benefits in Knowledge Management, the Antecedent of Online-Learning Strategies and Motivations: An Empirical Study," *Sustainability*, vol. 14, no. 5, p. 2570, Feb. 2022, doi: 10.3390/su14052570.
- [43] H. Abuhassna, W. M. Al-Rahmi, N. Yahya, M. A. Z. M. Zakaria, A. B. M. Kosnin, and M. Darwish, "Development of a new model on utilizing online learning platforms to improve students' academic achievements and satisfaction," *Int. J. Educ. Technol. High. Educ.*, vol. 17, no. 1, p. 38, Dec. 2020, doi: 10.1186/s41239-020-00216-z.
- [44] A. M. Maatuk, E. K. Elberkawi, S. Aljawarneh, H. Rashaideh, and H. Alharbi, "The COVID-19 pandemic and Elearning: challenges and opportunities from the perspective of students and instructors," *J. Comput. High. Educ.*, vol. 34, no. 1, pp. 21–38, Apr. 2022, doi: 10.1007/s12528-021-09274-2.
- [45] F. Li, Y. He, and Q. Xue, "Progress, Challenges and Countermeasures of Adaptive Learning," *Educ. Technol. Soc.*, vol. 24, no. 3, pp. 238–255, Dec. 2021, [Online]. Available: https://www.jstor.org/stable/27032868
- [46] A. Wullschleger *et al.*, "Improving the quality of adaptive learning support provided by kindergarten teachers in play-based mathematical learning situations," *Eur. Early Child. Educ. Res. J.*, vol. 31, no. 2, pp. 225–242, Mar. 2023, doi: 10.1080/1350293X.2022.2081348.
- [47] H. A. El-Sabagh, "Adaptive e-learning environment based on learning styles and its impact on development students' engagement," *Int. J. Educ. Technol. High. Educ.*, vol. 18, no. 1, p. 53, Dec. 2021, doi: 10.1186/s41239-021-00289-4.
- [48] S. H. Moltudal, R. J. Krumsvik, and K. L. Høydal, "Adaptive Learning Technology in Primary Education: Implications for Professional Teacher Knowledge and Classroom Management," *Front. Educ.*, vol. 7, Feb. 2022, doi: 10.3389/feduc.2022.830536.
- [49] K. Daugherty, R. Morse, A. R. Schmauder, J. Hoshaw, and J. Taylor, "Adjusting the Future of Adaptive Learning Technologies via a SWOT Analysis," *Intersect. A J. Intersect. Assess. Learn.*, vol. 3, no. 2, 2022, doi: 10.61669/001c.36295.
- [50] D. Karandish, "7 Benefits of AI in Education -- THE Journal," *The Journal*, 2021. https://thejournal.com/articles/2021/06/23/7-benefits-of-ai-in-education.aspx (accessed Dec. 05, 2023).
- [51] K. Seo, J. Tang, I. Roll, S. Fels, and D. Yoon, "The impact of artificial intelligence on learner-instructor interaction in online learning," *Int. J. Educ. Technol. High. Educ.*, vol. 18, no. 1, p. 54, Dec. 2021, doi: 10.1186/s41239-021-00292-9.
- [52] F. Kamalov, D. Santandreu Calonge, and I. Gurrib, "New Era of Artificial Intelligence in Education: Towards a Sustainable Multifaceted Revolution," *Sustainability*, vol. 15, no. 16, p. 12451, Aug. 2023, doi: 10.3390/su151612451.
- [53] N. Rajawat, "The role of AI and blended learning in shaping the future of education The Hindu," *The Hindu*, 2023. https://www.thehindu.com/education/the-role-of-ai-and-blended-learning-in-shaping-the-future-of-

education/article67060303.ece (accessed Dec. 05, 2023).

- [54] S. Zamir, Z. Yang, H. Wenwu, and U. Sarwar, "Assessing the attitude and problem-based learning in mathematics through PLS-SEM modeling," *PLoS One*, vol. 17, no. 5, p. e0266363, May 2022, doi: 10.1371/journal.pone.0266363.
- [55] H. Hendriana, T. Johanto, and U. Sumarmo, "The role of problem-based learning to improve students' mathematical problem-solving ability and self confidence," *J. Math. Educ.*, vol. 9, no. 2, pp. 291–299, 2018, doi: 10.22342/jme.9.2.5394.291-300.
- [56] N. Klang, N. Karlsson, W. Kilborn, P. Eriksson, and M. Karlberg, "Mathematical Problem-Solving Through Cooperative Learning—The Importance of Peer Acceptance and Friendships," *Front. Educ.*, vol. 6, Aug. 2021, doi: 10.3389/feduc.2021.710296.
- [57] R. Luczak and R. Erwin, "Mathematical modeling: a study of multidisciplinary benefits in the math classroom," *Teach. Math. its Appl. An Int. J. IMA*, Dec. 2022, doi: 10.1093/teamat/hrac021.
- [58] S. Chamberlin, A. M. Payne, and T. Kettler, "Mathematical modeling: a positive learning approach to facilitate student sense making in mathematics," *Int. J. Math. Educ. Sci. Technol.*, vol. 53, no. 4, pp. 858–871, Apr. 2022, doi: 10.1080/0020739X.2020.1788185.
- [59] C. Ledezma, A. Breda, and V. Font, "Prospective Teachers' Reflections on the Inclusion of Mathematical Modelling During the Transition Period Between the Face-to-Face and Virtual Teaching Contexts," *Int. J. Sci. Math. Educ.*, Aug. 2023, doi: 10.1007/s10763-023-10412-8.
- [60] Y. Wei, Q. Zhang, and J. Guo, "Can Mathematical Modelling Be Taught and Learned in Primary Mathematics Classrooms: A Systematic Review of Empirical Studies," *Educ. Sci.*, vol. 12, no. 12, p. 923, Dec. 2022, doi: 10.3390/educsci12120923.
- [61] L. Chen *et al.*, "Direction of collaborative problem solving-based STEM learning by learning analytics approach," *Res. Pract. Technol. Enhanc. Learn.*, vol. 14, no. 1, p. 24, Dec. 2019, doi: 10.1186/s41039-019-0119-y.
- [62] E. Xu, W. Wang, and Q. Wang, "The effectiveness of collaborative problem solving in promoting students' critical thinking: A meta-analysis based on empirical literature," *Humanit. Soc. Sci. Commun.*, vol. 10, no. 1, p. 16, Jan. 2023, doi: 10.1057/s41599-023-01508-1.
- [63] F. Saadati and P. Felmer, "Assessing impact of a Teacher professional development program on student problemsolving performance," *ZDM – Math. Educ.*, vol. 53, no. 4, pp. 799–816, Aug. 2021, doi: 10.1007/s11858-020-01214-1.
- [64] S. L. Wismath and D. Orr, "The Canadian Journal for the Scholarship of Teaching and Learning Collaborative Learning in Problem Solving: A Case Study in Metacognitive Learning Collaborative Learning in Problem Solving: A Case Study in Metacognitive Learning," *Can. J. Scholarsh. Teach. Learn.*, vol. 6, no. 3, 2015, [Online]. Available: http://ir.lib.uwo.ca/cjsotl_rcacea%5Cnhttp://ir.lib.uwo.ca/cjsotl_rcacea/vol6/iss3/10
- [65] O. Karamustafaoğlu and H. M. Pektaş, "Developing students' creative problem solving skills with inquiry-based STEM activity in an out-of-school learning environment," *Educ. Inf. Technol.*, vol. 28, no. 6, pp. 7651–7669, Jun. 2023, doi: 10.1007/s10639-022-11496-5.
- [66] S. Wilder, "Parental involvement in mathematics: giving parents a voice," *Educ. 3-13*, vol. 45, no. 1, pp. 104–121, Jan. 2017, doi: 10.1080/03004279.2015.1058407.
- [67] C. Tomasetto, A. Mirisola, S. Galdi, and M. Cadinu, "Parents' math–gender stereotypes, children's self-perception of ability, and children's appraisal of parents' evaluations in 6-year-olds," *Contemp. Educ. Psychol.*, vol. 42, pp. 186–198, Jul. 2015, doi: 10.1016/j.cedpsych.2015.06.007.
- [68] F. Huang, Z. Huang, Z. Li, and M. Zhang, "Relationship between Parental Involvement and Mathematics Achievement of Chinese Early Adolescents: Multiple Mediating Roles of Mental Health and Mathematics Self-Efficacy," *Int. J. Environ. Res. Public Health*, vol. 18, no. 18, p. 9565, Sep. 2021, doi: 10.3390/ijerph18189565.
- [69] J. Dietrichson *et al.*, "Targeted school-based interventions for improving reading and mathematics for students with or at risk of academic difficulties in Grades K-6: A systematic review," *Campbell Syst. Rev.*, vol. 17, no. 2, Jun. 2021, doi: 10.1002/CL2.1152.
- [70] E. Khasawneh, C. Gosling, and B. Williams, "What impact does maths anxiety have on university students?," *BMC Psychol.*, vol. 9, no. 1, p. 37, Dec. 2021, doi: 10.1186/s40359-021-00537-2.
- [71] N. Wang, A.-L. Tan, X. Zhou, K. Liu, F. Zeng, and J. Xiang, "Gender differences in high school students' interest in

STEM careers: a multi-group comparison based on structural equation model," *Int. J. STEM Educ.*, vol. 10, no. 1, p. 59, Oct. 2023, doi: 10.1186/s40594-023-00443-6.

- [72] F.-K. Chiang, Z. Tang, D. Zhu, and X. Bao, "Gender disparity in STEM education: a survey research on girl participants in World Robot Olympiad," *Int. J. Technol. Des. Educ.*, May 2023, doi: 10.1007/s10798-023-09830-0.
- [73] E. Makarova, B. Aeschlimann, and W. Herzog, "The Gender Gap in STEM Fields: The Impact of the Gender Stereotype of Math and Science on Secondary Students' Career Aspirations," *Front. Educ.*, vol. 4, Jul. 2019, doi: 10.3389/feduc.2019.00060.
- [74] L. Froehlich *et al.*, "Gender Stereotypes and Expected Backlash for Female STEM Students in Germany and Japan," *Front. Educ.*, vol. 6, Jan. 2022, doi: 10.3389/feduc.2021.793486.
- [75] R. Weinhandl *et al.*, "Utilising personas as a methodological approach to support prospective mathematics teachers' adaptation and development of digital mathematics learning resources," *J. Math. Teach. Educ.*, Nov. 2023, doi: 10.1007/s10857-023-09607-1.
- [76] D. Potari, "Mathematics teacher professional learning and teacher education practices," *J. Math. Teach. Educ.*, vol. 24, no. 3, pp. 227–230, Jun. 2021, doi: 10.1007/s10857-021-09501-8.
- [77] H. Gaspard, C. Parrisius, B. Nagengast, and U. Trautwein, "Understanding the interplay between targeted motivation interventions and motivational teaching practices in mathematics classrooms," *ZDM Math. Educ.*, vol. 55, no. 2, pp. 345–358, Mar. 2023, doi: 10.1007/s11858-022-01446-3.